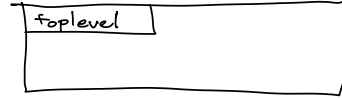
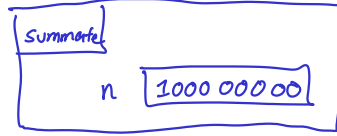
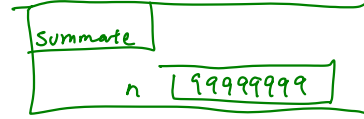
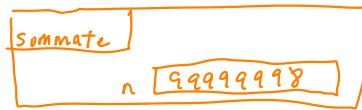


```

let rec Summate n =
  if n = 1 then 1 else
  n + Summate (n-1)
;;
Summate 100000000

```



```

let rec Summate n =
  if n = 1 then 1 else
  n + Summate (n-1)
;;

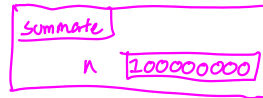
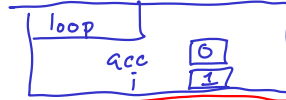
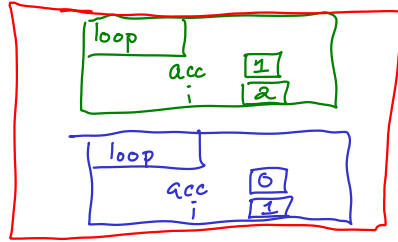
```

$$\left(100000000 + \left(99999999 + \left(\text{if } 99999998 = 1 \text{ then } 1 \text{ else } 99999998 + \text{Summate}(99999998 - 1) \right) \right) \right)$$

```

let Summate n =
  let rec loop acc i =
    if i = n + 1 then
      acc
    else
      loop (acc + i) (i + 1)
  in
  loop 0 1
;;
Summate 100000000

```

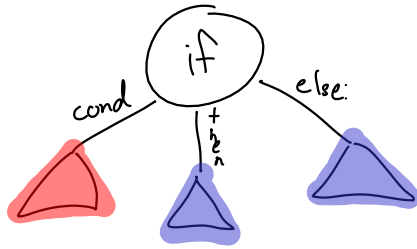


```

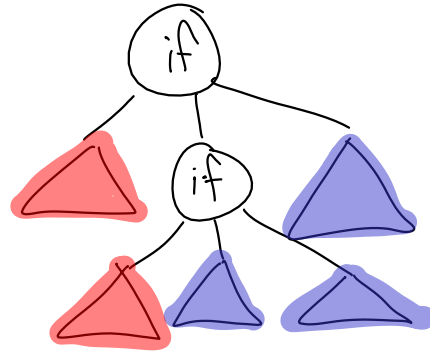
let rec loop acc i =
  if i = 100000000 + 1 then
    acc
  else
    loop (acc + i) (i + 1)
in
if 3 = 100000000 + 1 then
  3
else
  loop (3 + 3) (3 + 1)

```

A subexpression is a "tail expression" of a larger expression if the tail expression is the last thing the larger expression computes and the tail expression produces the result of the larger expression.



■ tail
■ non-tail

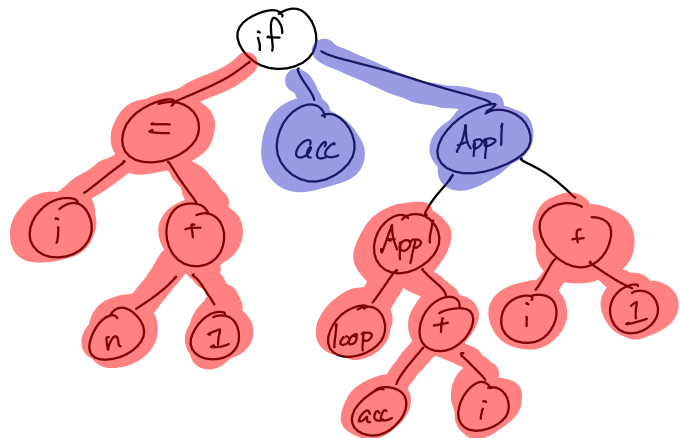


```

type expr =
  | EInt of int
  | EBool of bool
  | EUnaryOp of unary_operator * expr
  | EBinaryOp of binary_operator * expr * expr
  | ETuple of expr list
  | ELet of string * expr * expr
  | EVar of string
  | EIf of expr * expr * expr
  | EAppl of expr * expr
  | ESet of expr * expr * expr
  
```

```

let rec loop acc i =
  if i = n+1 then
    acc
  else
    loop (acc+i) (i+1)
in
  
```



"Tail call" is a call which is a tail expression