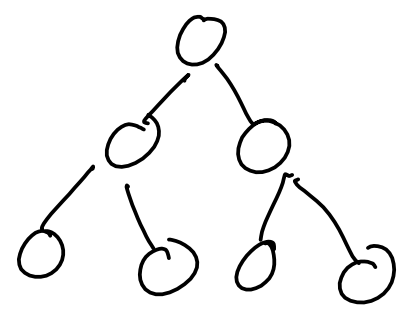


BST each node carrying  $K, V$

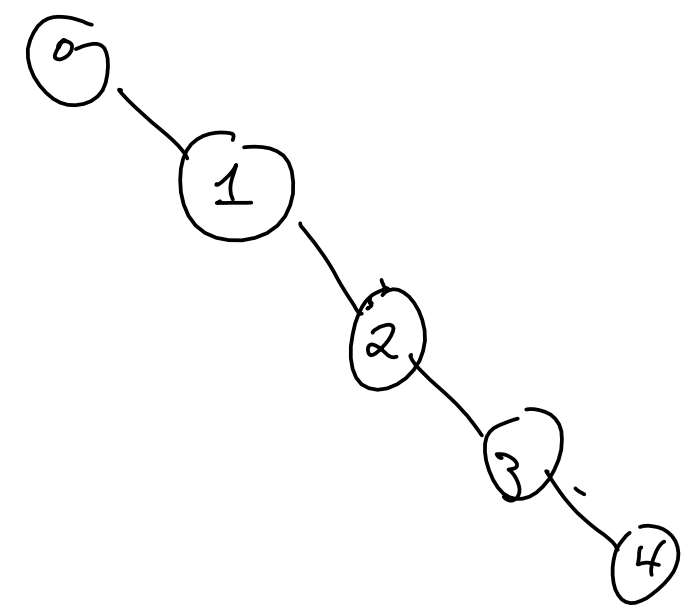
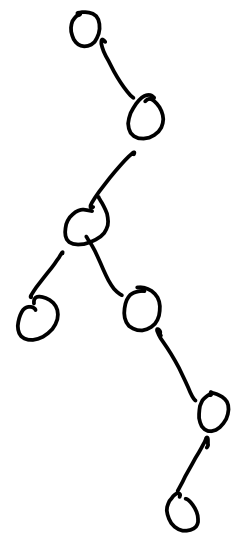
Impl of ADT  
"dictionary"

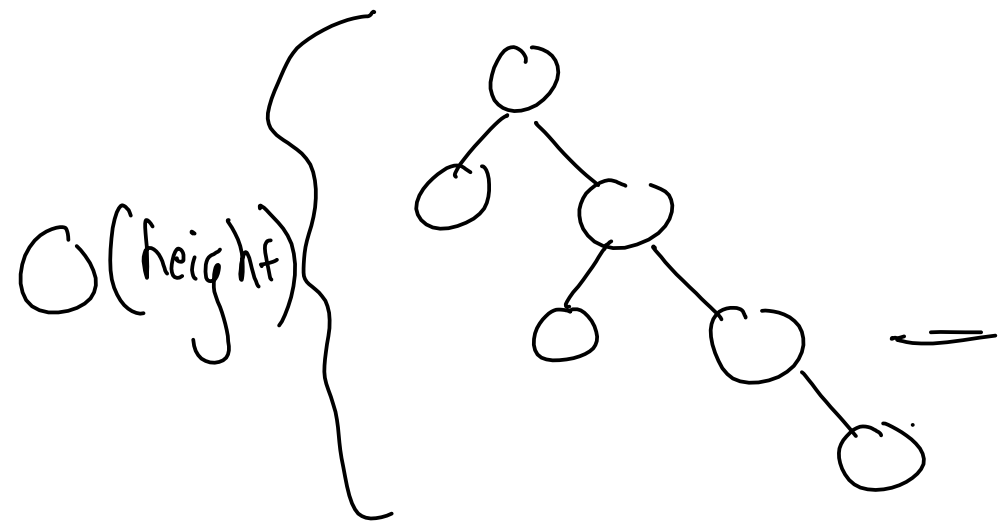
left  $K <$  this  $K <$  right  $K$



$n = 7 \sim 3$  steps  
 $2^3 = 8$

"Full"

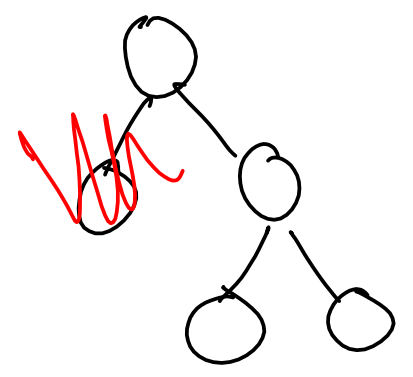




Lookups  $O(\log n)$   
Updates  $O(\log n)$

↑  
"includes fixing"  
the tree

We'd like for height to be  $O(\log n)$

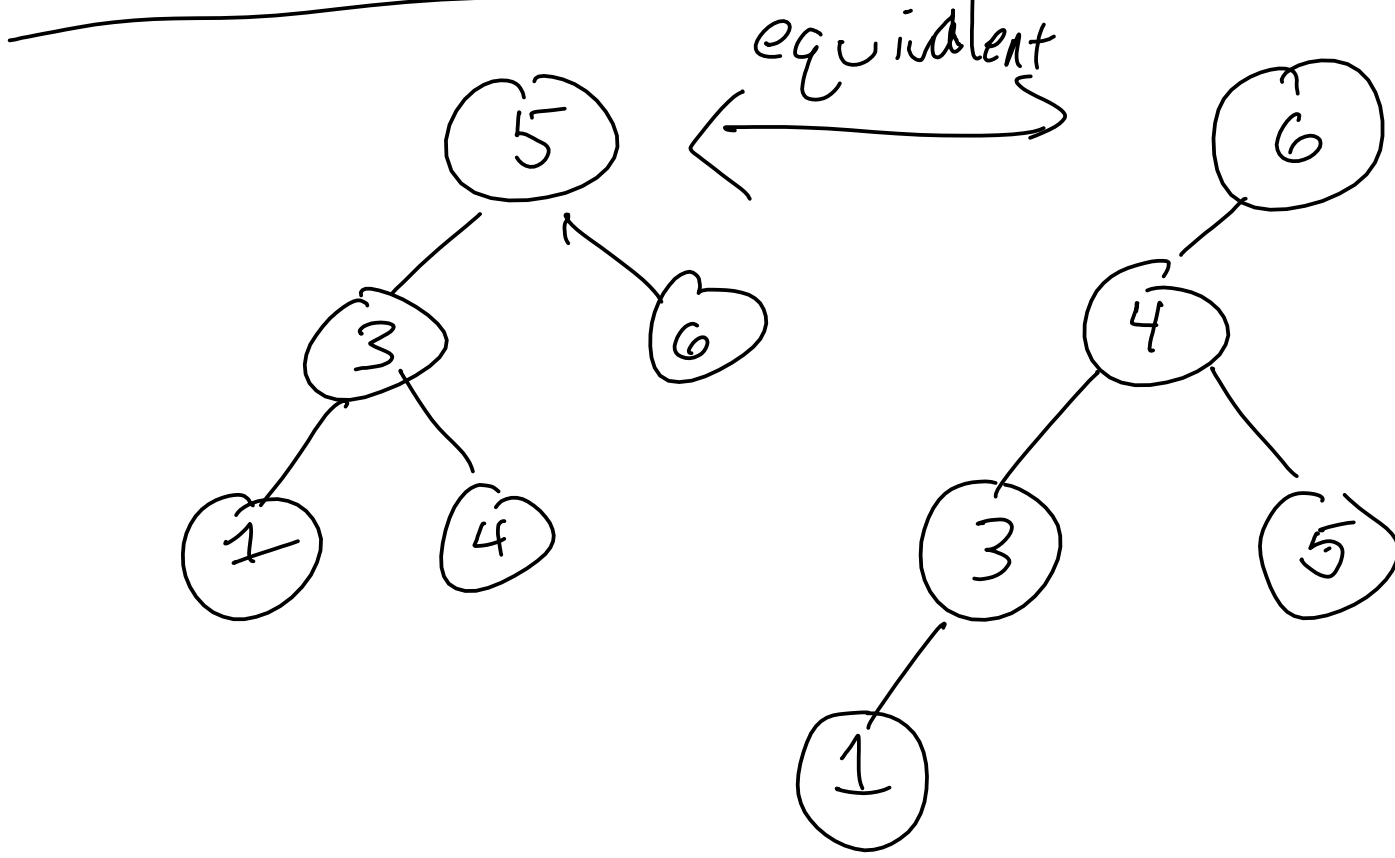
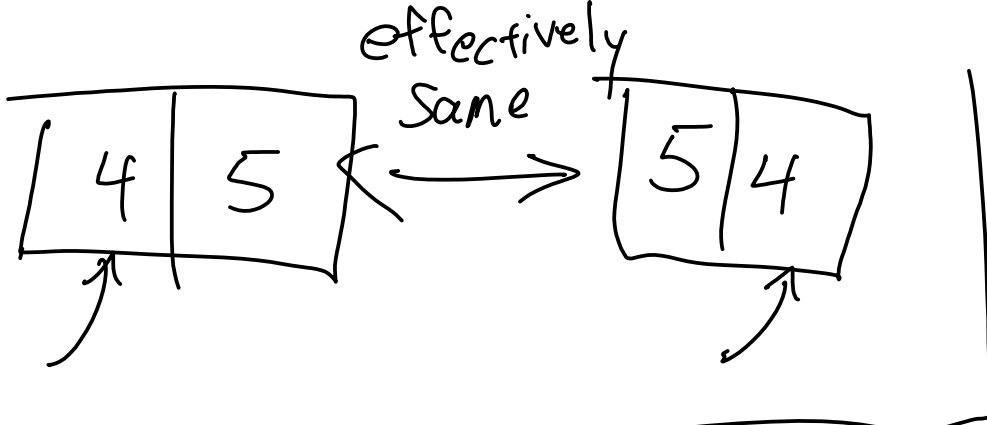


AVL Tree is a BST that stays "balanced"

Balanced: for any node: height(left child) and height(right child) differ by at most 1

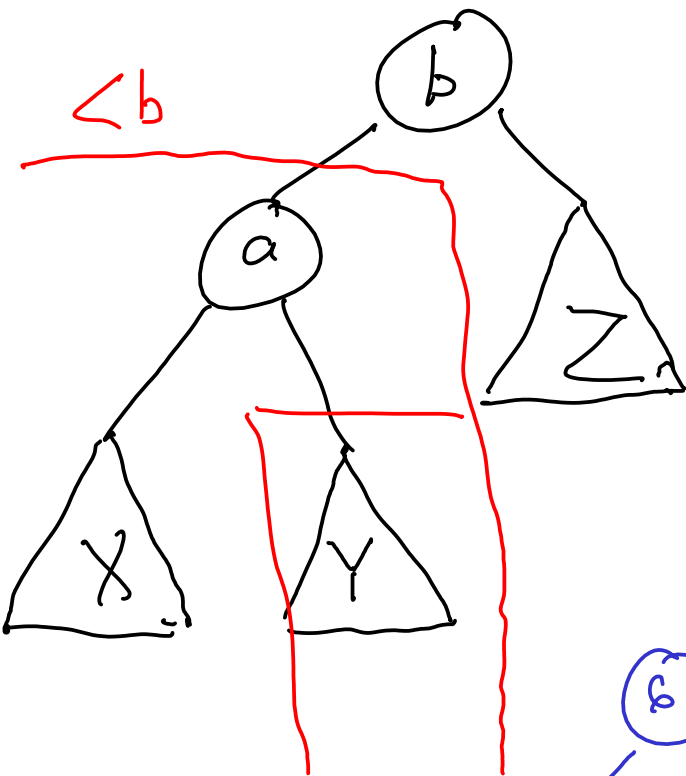
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Rotation

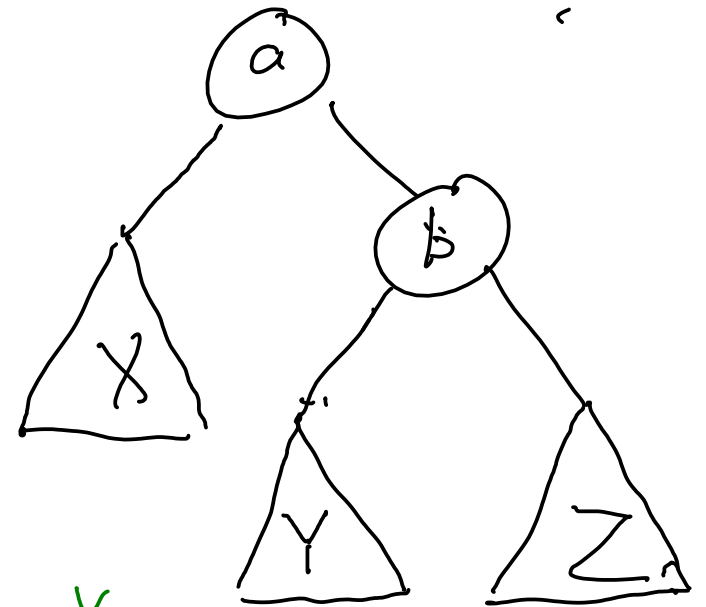


A tree rotation converts one (bin) tree to another

2 kinds: left right



Right Rotation.



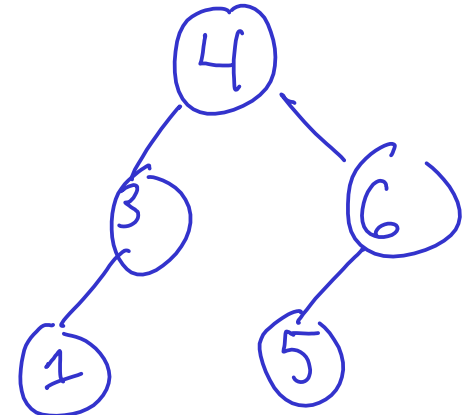
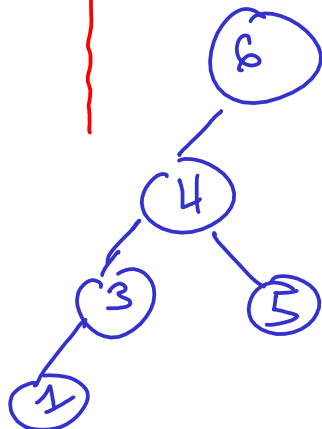
let  $a = 4$

let  $b = 6$

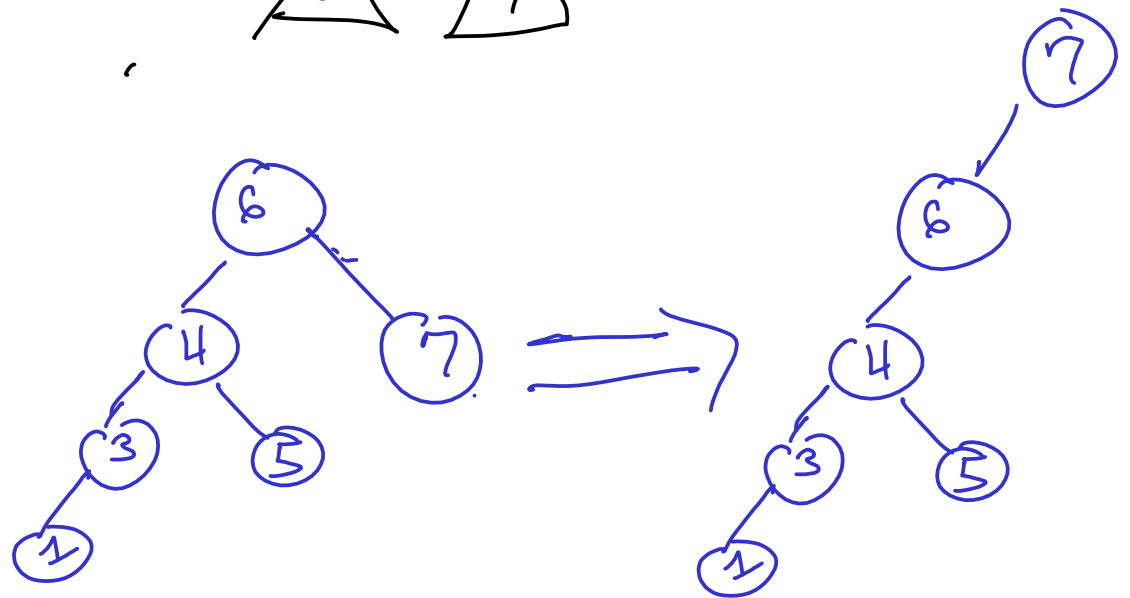
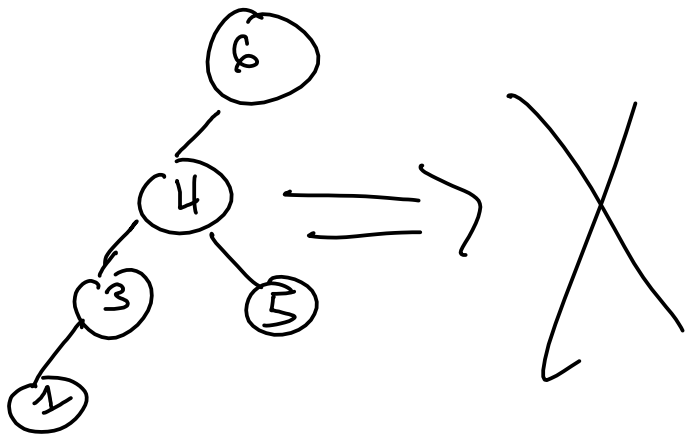
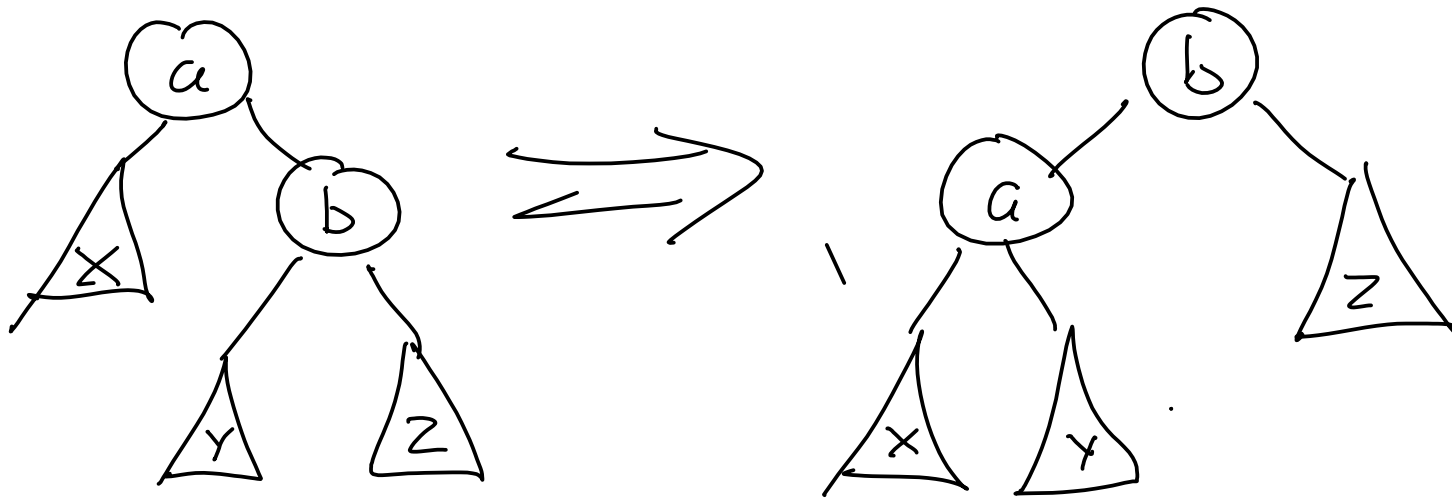
let  $X =$

let  $Y = 5$

let  $Z = *$



# Left Rotation



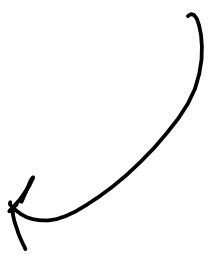
AVL invariant:  $|\text{left height} - \text{right height}| \leq 1$

template.  $\langle \text{typename } K, \text{typename } V \rangle$

class AVLTreeNode

K key;  
V value;  
... left;  
... right;  
int height;

change when tree changes  
add remove  
rotate



# Rebalancing

Method Insert (key, value) =

If this → key < key :

If this → right ≠ NULL :

this → right → Insert (key, value)

→ rebalance()

Else :

this → right = new Node (key, value)

recompute height

Else :

...

	Difference	
Left	Old	New
empty	0	1
single	1	0

