

# Hash Tables

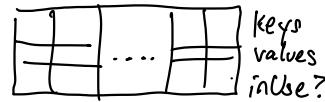
- an implementation of Dictionary (unique keys)

- int hash(K key)

- hash, modulus → pick a location in an array

- collision: multiple mappings want in same slot

- linear probing: use next empty slot



- forward chaining

## Dictionaries

AVL trees

get  
insert  
update  
remove

$O(\log n)$

Hash tables

average  $O(1)^*$

Linear Dictionary

$O(n)$   
using a list

Method `get(K key):`

For i in 0 up to `contents.size() - 1`:

If `contents[i].key == key`:

  Return `contents[i].value`

End If

End For

||

End Method

Method `insert(K key, V value):`

For i in 0 up to `contents.size() - 1`:

If `contents[i].key == key`:

  ||

End If

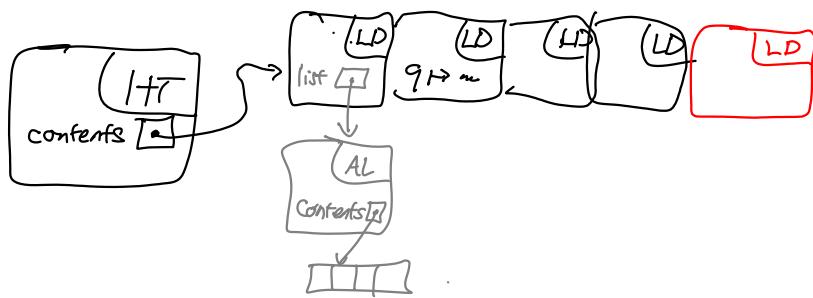
End For

`contents.insertLast(pair(key, value))`

End Method

Forward chaining hash table:

- array of LinearDictionary

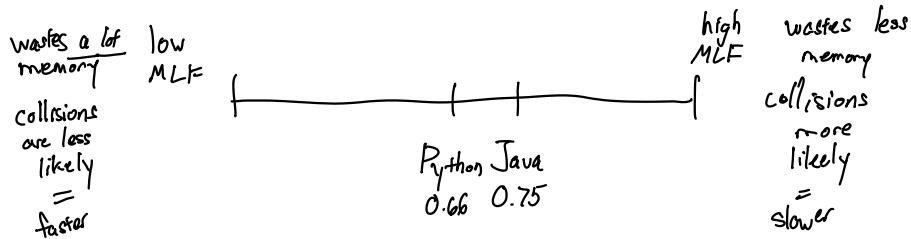


$n$  LDs  $\rightarrow$   $n$  mappings per LD

- array of LDs ("buckets")
- key/value pairs insert into LDs based on key hash
- when I have "too many" k/v pairs for the LDs I have, expand capacity of HT
  - make new LD array of twice the size
  - rehash and add all k/v pairs to the new array

$$\frac{\# \text{ of mappings}}{\# \text{ of buckets}} = \text{load factor}$$

max load factor  
(MLF)



1	→ "one"

insert (1, "one")  
 insert (5, "five")  
 insert (0, "zero")  
 insert (7, "seven")

$$MLF = 0.6$$

if your hash  
function is any good

1	→ "one", 5 → "five"

0	→ "zero", 1 → "one"
5	→ "five", 7 → "seven"

0	→ "zero", 1 → "one", 5 → "five", 7 → "seven"

Average

O(1)

- amortization
- averaging over all possible sets of user input