

ADT - List $\langle T \rangle$

... get(int index)

List $\langle int \rangle$

[5, 7, 8, 2]

ADT - Dictionary $\langle K, V \rangle$
(unique) key value

a dictionary is a collection of key-value mappings
all keys are unique

Dictionary $\langle string, int \rangle$

{ "a" \mapsto 5,
"b" \mapsto 7,
"cat" \mapsto 2,
"dog" \mapsto 7
}

V get(K key)

void insert(K key, V value)

void update(K key, V value)

} put(K, V)

V remove(K key)

int getSize()

bool contains(K key)

List $\langle K \rangle$ getKeys()

for today: assume K is ordered

Parallel List Dictionary

- list of keys
- list of values

- at a given index, key \mapsto value

A | C | Q | X

2 | 7 | 4 | 3

Array Dictionary

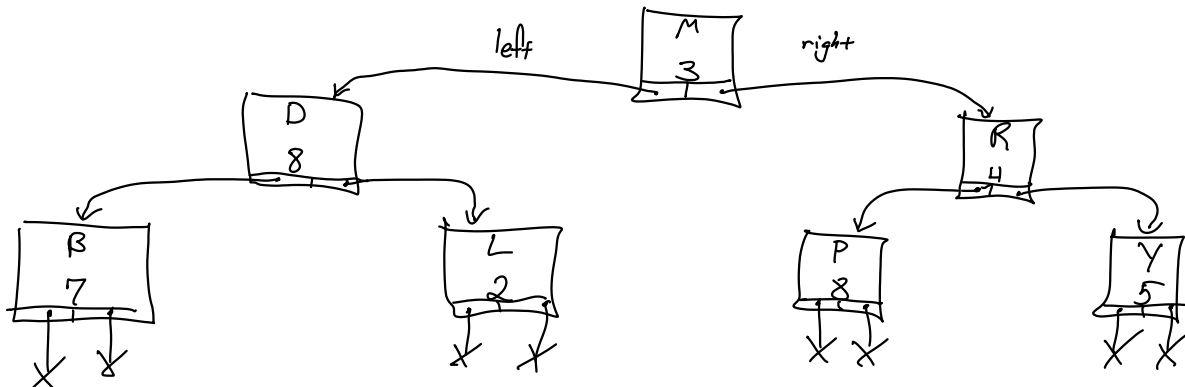
A | C | Q | X
2 | 7 | 4 | 3

Sorted Array Dictionary

+ invariant: array is always sorted

get(K): $O(\log n)$

insert(K, V): $O(n)$



Tree: a collection of nodes related to each other in the form above

Node: a member in a tree

Root: the node with no nodes above it (no parent)

Parent: the node immediately above a given node

Child: a node below a given node

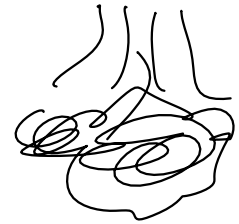
Leaf: a node with no children

Descendant: any node below a given node

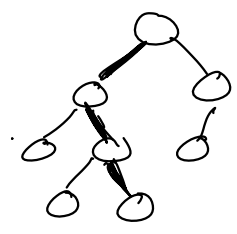
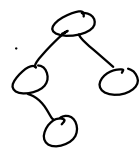
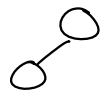
Ancestor: any node above a given node

Size: the number of nodes

Height: the number of steps between root & furthest leaf



x



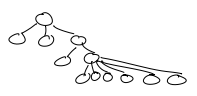
-1



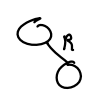
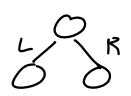
1

2

3



Binary tree: a tree where each node has at most one left child and one right child

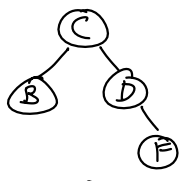


Binary Search Tree (BST):

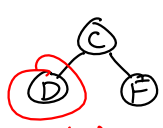
a binary tree where the key in any node is greater than the key in all of its left descendants and the key in any node is less than the key in all of its right descendants



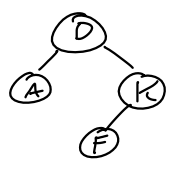
BST



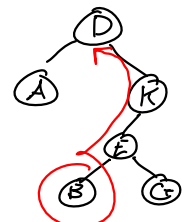
BST



not a BST



BST



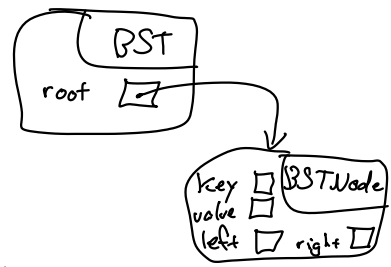
not a BST

BST invariant

Method get(K key):

Return getInSubtree(key, this → root)

EndMethod



Method getInSubtree(K key, BSTNode<K, V>* node):

If (node == null ptr):



Else If (key == node → key):

Return node → value;

Else If (key < node → key):

Return getInSubtree(key, node → left)

Else :

Return getInSubtree(key, node → right)

End If

EndMethod