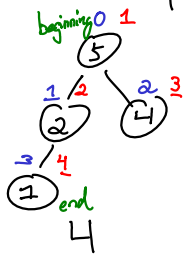
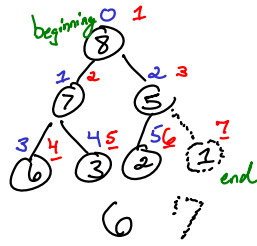


Complete Array Binary Tree

In a complete tree, the number of nodes describes its shape (and vice versa).



0	1	2	3
5	2	4	1



0	1	2	3	4	5
8	7	5	6	3	2

Given the index of a node, what is the index of its parent?

Given the index of a node, what are the indices of its children?

Given the index of a node, is it a leaf?

$$\text{parent}(n) = \left\lfloor \frac{n-1}{2} \right\rfloor$$

$$\text{parent}(n) = \left\lfloor \frac{n}{2} \right\rfloor$$

$$\text{leftChild}(n) = (n+1) \cdot 2 - 1$$

$$\text{leftChild}(n) = n \cdot 2$$

$$= 2n + 2 - 1 = 2n + 1$$

$$\text{rightChild}(n) = n \cdot 2 + 1$$

$$\text{rightChild}(n) = (n+1) \cdot 2 + 1 - 1$$

$$= 2n + 2 + 1 - 1 = 2n + 2$$

$$\text{isLeaf}(n) = \left\lfloor \frac{\text{size}}{2} \right\rfloor < n + 1$$

$$\text{isLeaf}(n) = \left\lfloor \frac{\text{size}}{2} \right\rfloor < n$$