

Depth-First Search

Function `reachableDFS(graph, src, dest) : bool`

Set frontier to new Stack

Set visited to new Set

`frontier.push(src)`

`visited.add(src)`

While frontier is not empty:

Set current to `frontier.pop()`

If `current == dest`:

→ Return true

EndIf

For each neighbor of current:

If neighbor not in visited:

`frontier.push(neighbor)`

`visited.add(neighbor)`

EndIf

EndFor

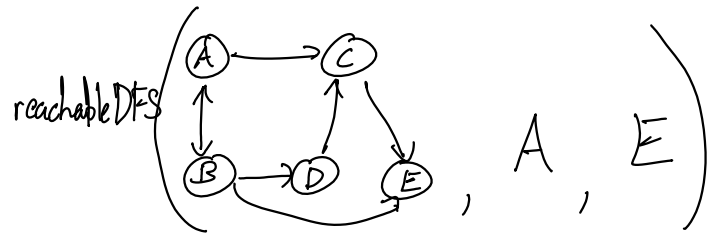
EndWhile

Return false

EndFunction

Set $\langle T \rangle$

Dictionary $\langle T, int \rangle$



current E
neighbor E

frontier

[B]

visited

{ A, B, C, E }

Breadth-First Search

Function `shortestLengthPath(graph, src, dst) : path`

Set frontier to new Queue

Set previous to new Dictionary from V to V

`frontier.enqueue(src)`

`previous.insert(src, src)`

While frontier is not empty

Set current to `frontier.dequeue()`

If `current == dst`:

Reconstruct path by following previous pointers

Return reconstructed path

End If

For each neighbor of current:

If neighbor is not a key in previous:

`previous.insert(neighbor, current)`

`frontier.enqueue(neighbor)`

End If

End For

End While

Return no path

End Function

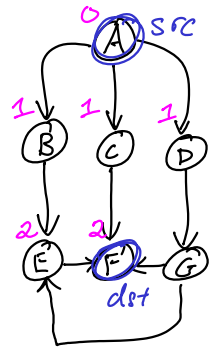
list of vertices

Initializing search frontier and accounting structures

result

exploration

]- result



frontier	D, E, F
previous	A → A, E → B B → A, F → C C → A, F → C D → A
current	C
neighbor	F

All-Lengths BFS

length of shortest path from src

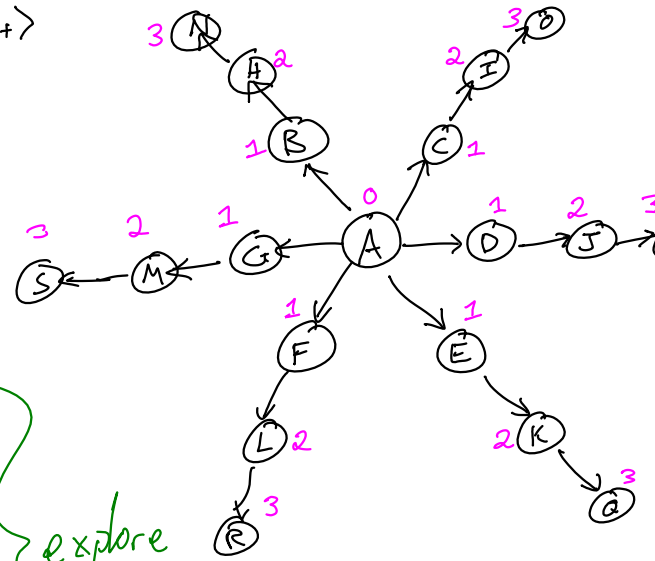
Function allLengthsBFS(graph, src) : Dictionary<V, int>

Set frontier to new Queue
 Set lengths to new Dictionary<V, int>
 frontier.enqueue(src)
 lengths.insert(src, 0)

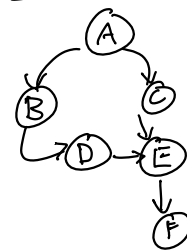
} init

→ While frontier is not empty:
 Set current to frontier.dequeue()
 For each neighbor of current:
 Set newLength to lengths.get(current) + 1
 IF neighbor is not a key in lengths:
 frontier.enqueue(neighbor)
 lengths.insert(neighbor, newLength)
 EndIF

EndFor
 EndWhile
 Return lengths results
 EndFunction



} explore



frontier:
 lengths: { A → 0, D → 2 }
 { B → 1, E → 2 }
 { C → 1, F → 3 }
 current: F newLength:
 neighbor:

Dijkstra's Algorithm (SSSP)

Function $\text{dijkstra's Lengths BFS}(\text{graph}, \text{src}) : \text{Dictionary} \langle V, \text{int} \rangle$

Set frontier to new ^{Min} Priority Queue $\langle \text{int}, V \rangle$

Set ~~lengths~~ ^{costs} to new Dictionary $\langle V, \text{int} \rangle$

frontier.enqueue(~~src~~) (0, src)

~~lengths~~ ^{costs}.insert(src, 0)

While frontier is not empty:

Set current to frontier.dequeue()

For each ~~neighbor~~ ^{outgoingEdge} of current:

Set neighbor to outgoingEdge.destination

Set stepCost to outgoingEdge

Set ~~newCost~~ ^{newCost} to ~~lengths.get(current)~~ ^{costs.get(current)} + ~~stepCost~~ ^{stepCost}

IF neighbor is not a key in ~~lengths~~ ^{costs}:

frontier.enqueue(~~neighbor~~) (newCost, neighbor)

~~lengths~~ ^{costs}.insert(neighbor, ~~newCost~~ ^{newCost})

Else IF ~~lengths.get(neighbor)~~ ^{costs.get(neighbor)} > newCost:

frontier.enqueue(newCost, neighbor)

costs.update(neighbor, newCost)

EndIF

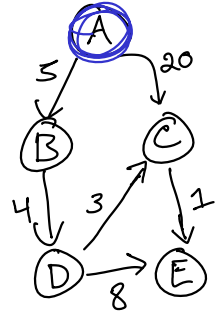
EndFor

EndWhile

Return lengths

EndFunction

dequeue only these vertices w/ best cost
require all edge weights to be non-negative



frontier:

costs: A → 0 D → 9
 B → 5 E → 13
 C → 12

current: C

outgoing Edge: C → E

neighbor: E newCost: 13

stepCost: 1